Short liverot documentation

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This doc is for the C++ version of livarot. The C version is just a dumb conversion, so the C++ classes become C structures, and the C++ member functions become C functions with the first parameter (called 1ui as often as possible) being the instance of the C structure on which the function is supposed to work, ie "this". Also the function names are mangled when 2 or more versions of the same C++ function exist.

1 Creating polygons

Obviously, before you manipulate polygons, you have to create them.

1.1 What's that Shape class?

It's defined in the Shape.h file.

A bunch of preliminary definitions for the mathematically impaired:

- Graph: a bunch of points and a bunch of edges between pairs of points. Edges can be directed (origin of the edge → end of the edge). Points can be called vertices.
- Planar: Wwhen a graph can be drawn in a 2D plane without intersection between edges, the graph is planar.
- Degree: the degree of a vertex in a graph is the number of edges having that point as end. In the case of directed graphs, the indegree is the number of edges whose end is the vertex, and the outdegree is the number of edges whose start is the vertex.
- Cycle: in a graph, a succession of vertices $v_0 \to v_1 \to \dots \to v_n \to v_0$ where each consecutive pair (v_i, v_{i+1}) is an edge of the graph. Usually, you request that each vertex only appears once in the cycle (exept the v_0 , of course, which appears twice).

• Eulerian: a graph is eulerian if you can find a cycle in the graph where each edge is visited exactly once. A nice characterization is that a undirected graph is eulerian if and only if each vertex has even degree, and a directed graph is eulerian if and only if the indegree of each vertex is equal to its outdegree.

In case this is still fuzzy, check the Boolean library documentation at http://www.xs4all.nl/~kholwerd/algdoc/datastructure.html.

A Shape is a polygon. More precisely, it can describe a polygon by treating it as a planar eulerian graph. Note that although the Shape class can store any graph, most of its functions require eulerian planar graphs. A Shape can describe any polygon, whith or without holes, with or without touching edges, etc...

And remember that Shapes are directed graphs.

1.2 What's that Path class?

It's defined in the Path.h file.

It's just a little helper class designed to store a path (surprised?), where a path is composed of the following possible elements:

- straight arcs (=segments)
- cubic bezier curves
- quadratic bezier curves, with any number of intermediary points
- elliptic arcs

Since these building blocks of a path are not all straight edges, they need to be converted in a polyline before being used to make polygon. Thus the Path class also contains a polyline approximation of the path it describes.

1.3 Winding numbers

A polygon splits the plane in a certain number of region. Each region has a winding number, which will be used in several places. For undirected graphs, the winding number of a point (any point of the given region) is the minimum number of edges you have to cross when going from this point to a point infinitely far away, not necessarily using a straight line. For directed graphs, edges have a left and a right side, and winding numbers are computed differently: the winding number of a point is the number of edges you have to cross from left to right minus the number of edges you have to cross right to left when going from the point to a point infinitely far away.

A fill rule is a rule according which to choose which region are "in the polygon" and which region aren't. The most used are the "odd-even" fill rule, where all regions with odd winding number are used, and the "non zero" fill rule, where all regions with winding number $\neq 0$ (positive or negative) are used. In livarot, the ConvertToShape function also accepts the "strictly positive" fill rule, where only the regions with strictly positive winding number are used.

An illustration of winding number can be found here: http://developer.apple.com/documentation/Cocoa/Conceptual/DrawBasic/Concepts/bezier.html#/apple_ref/doc/uid/20000886/CJBCCDGG (bottom of page)

1.4 How do i proceed?

You can build a polygon with different methods. The only requirement is that the Shape class instance you will use must describe a polygon. How you obtain that polygon is up to you ... Check the Tester.cpp file for examples.

1.4.1 Best method: path \rightarrow shape

Nearly all the functions mentioned below are member functions of the Path class.

First: build a Path: allocate it, build the path with the MoveTo, LineTo, CubicTo, etc...commands

Second: transform the path in a polyline with a call to Convert

Third: allocate a Shape class instance or use a pre-existing one.

Fourth: fill the polyline with a call to Fill or stroke it with a call to Stroke (possibly with dashes). These function take a dest argument which is the Shape instance which should contain the polygon.

Fifth: the polygon may contain self-intersections, duplicate points or edges, and other problems, meaning it's not a planar eulerian graph. A call to ConvertToShape will put a "good" version of the polygon in another Shape instance, the one you called ConvertToShape with; for example a->ConvertToShape(b) will compute a clean version of b and put it in a. Now you have a nice planar eulerian graph, ready to be used for subsequent operations.

Note: a path is only one contour. if you want to build a polygon with several contours (for example a polygon with holes), you have to add each contour incrementally. The justAdd parameter in the Fill and Stroke function allows that:

- if justAdd=false, the contents of the Shape class instance you pass as receiver for the polygon are erased: the result is a polygon containing only the contour associated with the Path.
- if justAdd=true, the contents are not erased, so that the contour associated to the Path is just added to the other contours already present in the Shape.

In case you need to make a hole, don't forget to invert the contour direction (see the winding rules section for the reason why); the invert boolean is currently disabled.

Note 2: sometimes you can guarantee that a contour doesn't have self-intersections or other problems. In these case, the ConvertToShape is overkill; you can just use the ForceToPolygon function on the Shape containing the contour(s) to say "that Shape is already a planar eulerian graph". Use with caution, though. Also note that almost all functions on the Shapes reorder the points in lexicographic order.

1.4.2 Not best method: directly build the contents of the Shape

You can add points and edges directly in the Shape instance.

First: start with a call to Reset() to empty the contents of the Shape

Second: add the points with calls to AddPoint(). The integer returned by the function is the ID of the point, more precisely its index in the pts array.

Third: add edges with calls to AddEdge(). The 2 parameters to this function are the points' IDs of its extremities.

Fourth: just like to other method, call ConvertToShape if needed.

2 I have a polygon. Now what?

Congratulations! Now you can do boolean operations on it or inset or offset it or raster it in a buffer.

2.1 Boolean operations

It's possible to do union, intersection, difference or symetric difference. The function Booleen is pretty self-explanatory, and returns a "good" polygon (planar eulerian blablabla).

2.1.1 Insets or Offsets

That's the MakeOffset function's job. After a call to MakeOffset, the calling instance of Shape will contain and offset of the polygon you pass in the of parameter. Note that this result is not a good polygon; you need a subsequent call to ConvertToShape to get a good polygon (or you can work directly on the bad polygon, if needed). Also note that you need the fill_positive fill rule to get the correct polygon.

2.1.2 Rasterization

Buffers are 32 bits ARGB and used through the very simple class Buffer. Rasterization comes in different flavours, with different algorithms, different paints, and clipping. Most are more or less equivalent in terms of speed. The rasterization functions are in the Buffer class. The helper function are static functions in the Buffer class also, and take care of manipulating colors, blending pixels and runs of pixels.

Available paints:

- straight color: stored in a std_color structure. The structure contains the color in ARGB format and in separate components formats (both in uint16_t and float format) for quicker rasterization. Maybe i'll add some gamma correction someday.
- linear gradient: stored in a lin_grad structure. Can have any orientation, size, number of stops, repeat pattern. The current implementation even accepts transparency.
- radial gradient: stored in a rad_grad structure. Like the linear gradient, any orientation, sizes, number of stops,etc ...
- generic paint: stored in a gen_color structure; basically it's just a set of callbacks, so you'll have to write them. There's a function to put the "current" position to a point, to a x-coordinate, to a y-coordinate, to the next pixel in the line, and a function to retrieve the color. No particular example yet.

Available methods (all are scanline algorithms):

- RasterShape: computing the line's exact coverage, then the pixels coverage, then rasterizing runs of pixels. The slowest. The quick parameter selects a different method to move the scanline. Sadly, it's often slower than the non-quick method. Don't use.
- RasterShapeA: computing the line's exact coverage, by means of a set of increments/decrements, then the pixels coverage, then rasterizing runs of pixels. Faster than the previous. I think libart uses the same method.
- RasterShapeB: uses 4*4 supersampling and bit masks. Converts the bitmasks to the same pixel runs format as the 2 previous functions, so that the blending functions can be reused. Can be overall faster than the 2 other method, since for even-odd and non-zero fill rule, this method can deal with non-"good" polygons, thus sparing you a call to ConvertToShape (slow function).

Blending functions:

• composition/decomposion of colors in ARGB format: Decomp and Recomp. Their parameters are self-explanatory.

- blending of a pixel on another one: Composite and CompositeOpaque variant. The "opaque" version assumes the color is blended on an already opaque pixel.
- blending of runs of pixels: RasterRun variants (one for each possible paint).

3 From Path to Shape and back

The "tenth" release adds a function to recover a Path from a correct Shape: the ConvertToForme() function. There are 2 version of this function:

- the basic one:void ConvertToForme(Path* dest);
- the complex one:void ConvertToForme(Path* dest,int nbP,Path* *orig);

The difference lies in the output, *ie* the Path stored in dest upon return. In the basic case, the Path is just a polyline, meaning it's a set of contours. In the complex one, the function tries to reassemble segments of the contours in curve patches. For that reason, it requires the Path from which the segments come. To use this method, you must do the following:

- for each Path that will create segments in the polygon, use ConvertWithBackData() instead of Convert(). This will prepare the Paths and make reassembling segments possible.
- assign an ID to each Path, and use Fill(dest, ID,...) when transforming it in a polygon. This is needed to find where each segment in the resulting polygon will come from.
- do the operations you need on the polygon. Only ConvertToShape() and Booleen() preserve the information needed for the reassembly, so you must limit yourself to these 2 functions.
- call void ConvertToForme(Path* dest,int nbP,Path* *orig);, where orig is an array of size nbP giving the correspondence between ID and Path. A segment with ID k will be reassembled according to the Path in orig[k].

4 Algorithmical remarks

4.1 Intersector

It's the usual Benley-Ottman sweepline intersector, with some rounding along the line of the Hobby algorithm; the windings are computed with a depth-first search in the graph. The rouding part is only "along the lines of", because i didn't really understand the implementation suggested by Hobby. The PolyBoolean seems truer to these suggestions, so check it out if needed. The Benley-Ottman uses an AVL tree and a binary heap queue, as it should.

That part should have a O((n+m)ln(n+m)) running time (where n is the number of points in the result polygon, and m the number of edges). This is quite optimal (i think), but remember that some non-"good" polygons have a "good" version where $m = n_0^2$ (n_0 being the number of points in the non-"good" original polygon).

The Booleen function uses the same intersector algorithm, only the winding computation and edge selection is different.

4.2 Rasterization

These functions have been written in a quite dumb way. Pixel manipulation ought to be severely optimized, vectorized or whatever. Also note that compiler ought to inline lots of the functions involved in this part.

4.3 Path handling

Also done very stupidly. The approximation of the bezier curves is done by recursive dichotomy. There is a maximum of 8 levels of recursion, feel free to increase it.

5 Before i leave

5.1 Rotating, translating,... polygons

Well, just apply the transformation to each element of the pts array of the Shape instance where the polygon is stored... the number of points is stored in nbPts.

A few caveats: if the transformation is an anti-transformation (for example: an axial symetry), all edges have to be reversed. Use the Inverse() function on each edge index, that is 0 to nbEdge-1. If the transformation is a nasty one, such as a whirl, you may end up with intersecting edges; a ConvertToShape will be needed. Of course, affine transformation are NOT nasty. You usually won't need to call SortPoints yourself, it's called by each function that requires the points in ordered form. Same thing for the SortEdge function, which sort the edges incident to each vertex in clockwise order.

5.2 Voronois

Are not implemented in the livarot version "eighth" and "ninth", but are in the previous ones. The Shape class changed slightly in the "eighth" version, and i still haven't rewritten the voronoi part.

It's back in "tenth", but still no clipping of diagrams against polygons, nor rasterization of these diagrams.

5.3 Justification

That part is just for fun. It's in livarot 'cause i used the polygon function to make justification in arbitrary shapes possible, but it has nothing to do with it... sadly, my poor understanding of how sourceforge.net file releases work had me delete that part. It's gone for now

5.4 What to include?

LivarotDefs.h contains the basic constants and general types. Livarot.h contains the includes for the appropriate classes.